



# Binding of ammonia to small copper and silver clusters

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## Abstract

We report equilibrium geometries, harmonic frequencies, and thermochemical data for the metal cluster–ammonia complexes  $\text{Ag}_n(\text{NH}_3)$  and  $\text{Cu}_n(\text{NH}_3)$  ( $n = 1, 2, 3, 4$ ),  $\text{Ag}_4(\text{NH}_3)_2$ , and  $\text{Cu}_4(\text{NH}_3)_2$  calculated by a density functional method. The calculated shifts in ammonia umbrella mode frequency correlate with the observed shifts and the calculated enthalpies of complexation. The preferred site for  $\text{NH}_3$  adsorption and the calculated bond enthalpies can be rationalized by considering atomic charges obtained from a natural population analysis and polarization of the metal electron density. © 1999 Elsevier Science B.V. All rights reserved.

## 1. Introduction

Silver clusters have recently been studied with experiments probing the size dependence of reactivity towards ammonia. Rayner et al. have reviewed enthalpy and entropy changes for  $\text{NH}_3$  adsorption on metal clusters of varying size and spectroscopic data of metal cluster–ammonia complexes [1]. Detailed interpretation of experiments for structure elucidation and for a fuller understanding of the reactivity of these clusters requires correlation of experimental and theoretical results. This prompted us to study the ammonia complexes of silver clusters  $\text{Ag}_n$  ( $n = 1, 2, 3, 4$ ) by density functional theory (DFT). We also studied the corresponding copper cluster series in order to gain more insight into the physical chemistry of these systems. Our copper cluster calculations may also help understand some aspects of

ammonia adsorption on copper surfaces, a system that is currently the subject of experimental interest [2]. The number of electrons and importance of electron correlation in transition-metal clusters make DFT a natural choice. We tried various combinations of functionals, basis set, and effective core potential. In Section 2, we assess the accuracy of the method that we chose by comparing our calculations to structural, spectroscopic and thermochemical experimental data. This establishes a procedure which, we think, can provide reliable quantitative predictions in future computational investigations of larger clusters.

## 2. Methods and background information

Calculations were performed with GAUSSIAN 98 [3]. We chose the DFT functional specified by the keyword B3P86 for most calculations. This method combines Becke's three-parameter hybrid exchange functional [4] with Perdew's gradient-corrected cor-

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Table 1

Equilibrium bond lengths (Å), binding energies (eV), and harmonic vibrational frequencies ( $cm^{-1}$ ) for copper and silver dimer

Method	Cu <sub>2</sub>			Ag <sub>2</sub>		
	R <sub>e</sub>	D <sub>e</sub>	ω	R <sub>e</sub>	D <sub>e</sub>	ω
B3P86/DZVP	2.264	1.65	235	2.655	1.38	157
BP86/SDD	2.222	2.13	274	2.567	1.72	189
B3P86/SDD	2.224	1.92	271	2.562	1.59	191
Expt.*	2.220	2.01	266.4	2.53	1.66	192.4

\* Experimental data for Cu<sub>2</sub> taken from Ref. [14] and data for Ag<sub>2</sub> from Ref. [9].

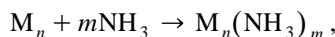
relation functional [5]. Our choice is motivated partly by the good results obtained with a similar functional – Becke's 1988 exchange [6] with Perdew's 1986 correlation [5] – in recent studies of complexes of copper [7,8] and silver [9] clusters, and partly by practical considerations: inclusion of Hartree–Fock exchange in the hybrid functional makes SCF convergence easier by increasing slightly the small HOMO–LUMO gap of metal clusters [10]. Furthermore, the hybrid B3LYP method yielded accurate dipole moments and infrared (IR) intensities in general [13], and accurate dipole polarizabilities in metal clusters [12]. As we will show, information on the reactivity of metal clusters can be obtained by analysing related properties – partial atomic charges and Raman intensities. Our preferred method, denoted B3P86/SDD, combines the Stuttgart–Dresden effective core potential (ECP) [11] for Ag and Cu with the D95\*\* basis set for ammonia. The ECP basis set describes explicitly 19 valence electrons by a contracted [6s,5p,3d] basis. The keywords specified in GAUSSIAN 98 jobs are 'B3P86/SDD', and 'extrabasis' to put polarization functions on the ligand and change the ammonia basis from D95 to D95\*\*.

We assessed the performance of the B3P86/SDD method by comparing calculated and experimental spectroscopic constants for Cu<sub>2</sub> and Ag<sub>2</sub> (see Table 1). The B3P86/DZVP method, which uses all-electron calculations with the DGAUSS-DZVP basis set [15], suffers large deviations from experimental values. The two sets of ECP calculations, BP86/SDD and B3P86/SDD, both yield estimates of the metal–metal bond lengths, dissociation energies and harmonic frequencies in close agreement with experiment. This shows the importance of including relativistic effects in Cu and Ag, even if only approxi-

mately by using an ECP. The B3P86/DZVP and B3P86/SDD methods are in qualitative agreement for the Raman and IR intensities of M<sub>n</sub>NH<sub>3</sub>. Hence, all geometry optimizations and harmonic vibrational calculations reported here were performed using the B3P86/SDD (ECP) method.

### 3. Structures and energetics

We consider the series of reactions



where M = Cu or Ag, and (n,m) are (1,1), (2,1), (3,1), (4,1), and (4,2). The optimized structures are sketched in Figs. 1 and 2, spatial and electronic

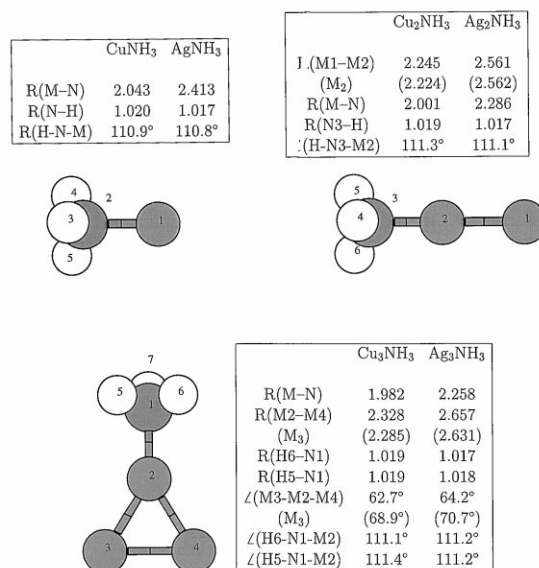


Fig. 1. Structure of the M<sub>n</sub>(NH<sub>3</sub>) clusters (M = Ag, Cu, and n = 1,2,3) and bond lengths in Å.

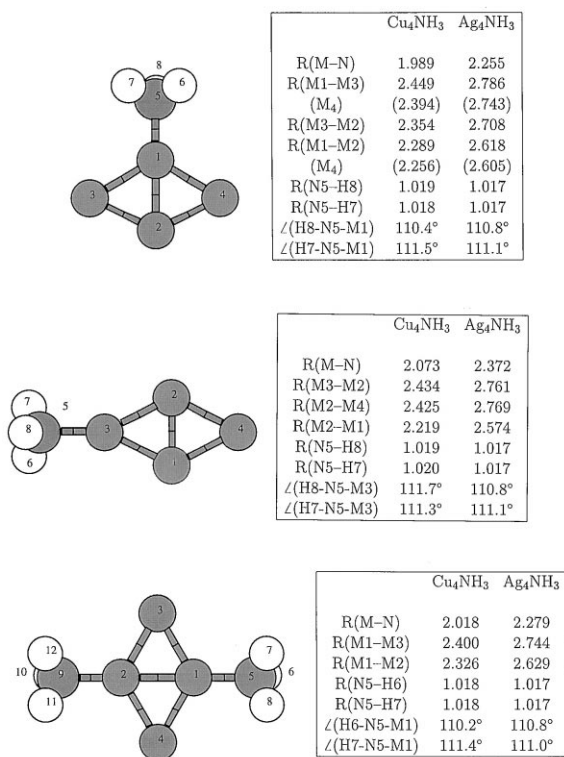


Fig. 2. Structure of the  $M_4(NH_3)_m$  clusters ( $M = Ag, Cu$ , and  $m = 1, 2$ ) and bond lengths in Å.

symmetries are given in Tables 2 and 3. Generally, small ligands can bind ‘atop’ one atom in the cluster, or to a ‘bridge’ site with local  $C_{2v}$  symmetry, or by

capping the center of a  $M_3$  triangular face. For electron–donor ligands, such as  $NH_3$ , the atop site is preferred on copper clusters [7] and platinum surfaces [16,17]. Likewise, adsorption of CO to atop sites of small platinum cluster is energetically favoured [18]. We did a few test calculations for adsorption sites other than atop and found that these species relaxed towards the atop geometry upon optimization. In the following, we consider only atop adsorption geometries.

$AgNH_3$  and  $CuNH_3$  have  $C_{3v}$  equilibrium structures. Their electronic state ( $^2A_1$ ) is non-degenerate and they do not distort to lower symmetry ( $C_{2v}$ ). The computed Ag–N stretching frequency is in good agreement with the value obtained from the A–X vibronic spectrum of the silver–ammonia stretching [19]. This lends support to assigning  $^2A_1$  as the ground state.  $M_2NH_3$  complexes have  $C_{3v}$  structures formed by binding the nitrogen end of ammonia to the atop site of the dimer. The equilibrium structure of ground state  $M_3$  was reported to be an obtuse isosceles triangle for copper [22] and silver [9]. Binding  $NH_3$  to  $M_3$  in an atop fashion leads to a  $C_s$  symmetry complex where one of the three N–H bond is in a plane perpendicular to the plane defined by  $M_3$  (see Fig. 1). Rotation of  $NH_3$  around the M–N axis gives rise to a  $C_s$  geometry where the symmetry plane is coplanar with  $M_3$ . The two structures are within  $5\text{ cm}^{-1}$  in energy, the torsional rotation of  $NH_3$  is essentially unhindered, and we report only one of the two isomers. Assuming free

Table 2

$Cu_n + NH_3$  adsorption thermochemical data (in kcal/mol, except the energy  $E$  (in au) and  $\Delta S$  (in cal mol<sup>-1</sup> K<sup>-1</sup>) at 298.15 K calculated by B3P86/SDD

	Sym	$E$	ZPE	$-\Delta E_{ad}$	$-\Delta H_{ad}$	$-\Delta S_{ad}$
$NH_3$	$C_{3v}/^1A_1$	-56.7528	21.8			
Cu		-197.7528	0			
$CuNH_3$	$C_{3v}/^2A_1$	-254.5291	23.5	13.1	13.7	23.9
$Cu_2$	$D_{2h}/^1A_1$	-395.5767	0.4			
$Cu_2NH_3$	$C_{3v}/^1A_1$	-452.3705	24.5	23.5	24.1	29.2
				> 25 <sup>a</sup>		
$Cu_3$	$C_{2v}/^2B_2$	-593.3682	0.8			
$Cu_3NH_3$	$C_s/^2A'$	-650.1703	25.0	28.4	28.9	26.9
$Cu_4$	$D_{2h}/^1A_1$	-791.2047	1.4			
$Cu_4NH_3$ (S)	$C_s/^1A'$	-848.0052	25.7	27.5	27.9	26.4
$Cu_4NH_3$ (L)		-847.9832	25.0	14.4	15.1	26.4
$Cu_4(NH_3)_2$	$C_{2v}/^1A_1$	-904.7964	49.7	22.0	22.3	30.2

<sup>a</sup> Experimental lower bound; see Ref. [20].

Table 3

Ag<sub>n</sub> + NH<sub>3</sub> adsorption thermochemical data (in kcal/mol, except the energy *E* (in au) and Δ*S* (in cal mol<sup>-1</sup> K<sup>-1</sup>)) at 298.15 K calculated by B3P86/SDD

	Sym	<i>E</i>	ZPE	−Δ <i>E</i> <sub>ad</sub>	−Δ <i>H</i> <sub>ad</sub>	−Δ <i>S</i> <sub>ad</sub>
NH <sub>3</sub>	C <sub>3v</sub> / <sup>1</sup> A <sub>1</sub>	−56.7528	21.8			
Ag		−147.4205	0			
AgNH <sub>3</sub>	C <sub>3v</sub> / <sup>2</sup> A <sub>1</sub>	−204.1873	23.2	7.5	8.1	20.8
Ag <sub>2</sub>	D <sub>2h</sub> / <sup>1</sup> A <sub>1</sub>	−294.8995	0.3			
Ag <sub>2</sub> NH <sub>3</sub>	C <sub>3v</sub> / <sup>1</sup> A <sub>1</sub>	−351.6821	24.1	16.7	17.2 16.4 ± 3 <sup>a</sup>	27.9
Ag <sub>3</sub>	C <sub>2v</sub> / <sup>2</sup> B <sub>2</sub>	−442.3482	0.5			
Ag <sub>3</sub> NH <sub>3</sub>	C <sub>s</sub> / <sup>2</sup> A'	−499.1371	24.5	20.6	21.3	29.7
Ag <sub>4</sub>	D <sub>2h</sub> / <sup>1</sup> A <sub>1</sub>	−589.8372	0.9			
Ag <sub>4</sub> NH <sub>3</sub> (S)	C <sub>s</sub> / <sup>1</sup> A'	−646.6265	25.0	23.2	21.0 14 <sup>b</sup>	23.6
Ag <sub>4</sub> NH <sub>3</sub> (L)		−646.6089	24.5	12.6	10.2	21.7
Ag <sub>4</sub> (NH <sub>3</sub> ) <sub>2</sub>	C <sub>2v</sub> / <sup>1</sup> A <sub>1</sub>	−703.4102	48.8	17.3	17.5	29.1

<sup>a</sup> Experimental value from Ref. [21].

<sup>b</sup> Experimental value from Ref. [1].

rotation of the NH<sub>3</sub> group, the symmetry effectively becomes C<sub>2v</sub>. In the rest of our discussion, existence of multiple rotamers of M<sub>n</sub>NH<sub>3</sub> and M<sub>n</sub>(NH<sub>3</sub>)<sub>2</sub> arising from different azimuth orientations of NH<sub>3</sub> is implied although we report a single geometry.

It is well established that the global minimum on the potential energy surface of Ag<sub>4</sub> assumes a D<sub>2h</sub> rhombic geometry [23,9]. Ligands can bind atop at either the short (S) or long (L) diagonal positions of the rhombus. The two structures are denoted Ag<sub>4</sub>(NH<sub>3</sub>) (S) and Ag<sub>4</sub>(NH<sub>3</sub>) (L) in Fig. 2. We also examined NH<sub>3</sub> binding to a higher energy isomer of M<sub>4</sub> formed by atop addition of M to triangular M<sub>3</sub> giving a C<sub>2v</sub> Y-shaped structure. Ammonia prefers to bind in an atop way to the metal atom which is not in the triangle, the one with lower coordination. However, this structure transforms into the rhombic isomer upon optimization and is excluded from our analysis. Three isomers of M<sub>4</sub>(NH<sub>3</sub>)<sub>2</sub> can be formed by attaching NH<sub>3</sub> to different atop sites: we label them SS, LL, and SL according to the diagonals of the rhombus. We show the most stable isomer M<sub>4</sub>(NH<sub>3</sub>)<sub>2</sub> (SS) in Fig. 2. The LL and SL structures are unstable, they are not minima of the potential energy surface and distort upon geometry optimization.

Our theoretical estimates of enthalpy and entropy changes for adsorption on Cu<sub>n</sub> and Ag<sub>n</sub> clusters are in Tables 2 and 3. Ag<sub>2</sub>(NH<sub>3</sub>), Cu<sub>2</sub>(NH<sub>3</sub>), and Ag<sub>4</sub>(NH<sub>3</sub>) have been characterized experimentally [1,20]. There are very few possibilities for the structure of Ag<sub>2</sub>(NH<sub>3</sub>) (and Cu<sub>2</sub>(NH<sub>3</sub>)), and the linear Ag–Ag–NH<sub>3</sub> configuration was established by the agreement of theory and experiment [21]. A comparison of theoretical and experimental estimates of the bond enthalpies of M<sub>2</sub>(NH<sub>3</sub>) suggests that our calculated bond enthalpies are within a few kcal/mol of the true values and that the lower bounds obtained by the kinetic method of Lian et al. [20] are probably close to actual bond enthalpies. Information on the structure of other M<sub>n</sub>(NH<sub>3</sub>)<sub>m</sub> complexes is not directly available from experiments, therefore we can not definitively assess the accuracy of our calculated bond enthalpy for Ag<sub>4</sub>(NH<sub>3</sub>).

The enthalpy change for adsorption of a single NH<sub>3</sub> ligand ranges from −14 to −28 kcal/mol for copper clusters, and from −8 to −21 kcal/mol for silver clusters<sup>1</sup>. The strength of the metal–ligand

<sup>1</sup> We estimate the counterpoise correction to basis set superposition error on these values to be less than 1 kcal/mol.

bond is intermediate between strong physisorption and weak chemisorption<sup>2</sup>. Since the Mulliken analysis gives metal–N bond orders smaller than 0.2, the ammonia is best described as ‘strongly physisorbed’ on the metal clusters. For both series of reactions,  $\Delta H_{\text{ad}}$  increases with cluster size from  $\text{MNH}_3$  to  $\text{M}_3\text{NH}_3$ . The calculated  $\Delta H_{\text{ad}}$  for  $\text{M}_3\text{NH}_3$  and  $\text{M}_4\text{NH}_3$  (S) are roughly equal. Adsorption of a second  $\text{NH}_3$  on  $\text{M}_4\text{NH}_3$  (S) to give  $\text{M}_4(\text{NH}_3)_2$  (SS) is less exothermic by 4–6 kcal/mol. The entropy change accompanying  $\text{NH}_3$  adsorption varies from  $-20$  to  $-30$  cal mol<sup>-1</sup> K<sup>-1</sup> for both  $\text{Cu}_n$  and  $\text{Ag}_n$ . The large entropy decrease is mainly caused by the loss of the three translational degrees of freedom. These translations become vibrational modes in the complex, resulting in an increase of vibrational entropy that is larger when the vibrational mode frequencies are smaller. Therefore, a relatively small entropy decrease is indicative of a floppy  $\text{M}_n\text{NH}_3$  complex.

The geometries of the metal clusters change very little upon  $\text{NH}_3$  adsorption. Typically, the metal–metal bond lengths increase by 0.05–0.10 Å and the overall structure is retained. Likewise, the geometry of the adsorbed  $\text{NH}_3$  ligand is similar to that of the free ligand: the N–H bond lengths increase by less than 0.01 Å and the M–N–H angles are generally within 1° of the pyramidal angle of the free ligand (111.7°). Consistent with this, the structural reorganization energies are very small, less than 0.6 kcal/mol for the  $\text{M}_4$  moiety of  $\text{Cu}_4\text{NH}_3$  and  $\text{Ag}_4\text{NH}_3$ , and essentially zero for  $\text{NH}_3$ . Nonetheless, we see a correlation between the equilibrium M–N bond length and  $\Delta H_{\text{ad}}$ :  $R_e$  (M–N) decreases as binding becomes more exothermic.

The calculated values of  $\Delta H_{\text{ad}}$  and  $\Delta S_{\text{ad}}$  for  $\text{Ag}_2\text{NH}_3$  agree closely with the experimental values of Ref. [1]. This is reassuring and makes us confident about calculations for complexes that have not been characterized experimentally. The experimental value of  $\Delta H_{\text{ad}}$  for  $\text{Ag}_4\text{NH}_3$  ( $-14$  kcal/mol) is intermediate between our estimates of  $-21$  kcal/mol for the S structure and  $-10$  kcal/mol for the L structure.

The 7 kcal/mol apparent discrepancy between theory and experiment is somewhat surprising. We note, however, that  $\text{Ag}_4$  could not be observed because its ionization potential (IP) is too large for photoionization mass spectrometric detection [1]. Our calculated IPs for  $\text{Ag}_4$ ,  $\text{Ag}_4\text{NH}_3$ (S), and  $\text{Ag}_4\text{NH}_3$  (L) (7.09, 6.56, and 6.22 eV, respectively) raise the possibility that  $\text{Ag}_4\text{NH}_3$ (S) may not have been detected either and that the observed  $\text{Ag}_4\text{NH}_3$  species may be another isomer, possibly  $\text{Ag}_4\text{NH}_3$  (L). There is good agreement between B3P86/SDD theory and experiment on the blue shift of the  $\text{NH}_3$  inversion (or

Table 4  
Harmonic frequencies (cm<sup>-1</sup>), IR intensities (IR, in km/mol) and Raman intensities (Ram, in Å<sup>4</sup>/a.m.u.) of  $\text{Cu}_n\text{NH}_3$  and  $\text{Ag}_n\text{NH}_3$  ( $n = 1, 2, 3$ )

	$\omega$	IR/Ram	$\omega$	IR/Ram
	CuNH <sub>3</sub>		AgNH <sub>3</sub>	
M–N str	320 <i>a</i> l	3/111	213 <i>a</i> l	8/64
NH <sub>3</sub> roc	480 <i>e</i>	35/39	213 <i>a</i> l	3/37
NH <sub>3</sub> inv	1156 <i>a</i> l	142/54	1093 <i>a</i> l	153/12
	1650 <i>e</i>	26/26	1656 <i>e</i>	26/20
sym NH <sub>3</sub> str	3467 <i>a</i> l	36/1206	3500 <i>a</i> l	9/801
	3615 <i>e</i>	30/41	3653 <i>e</i>	23/44
	Cu <sub>2</sub> NH <sub>3</sub>		Ag <sub>2</sub> NH <sub>3</sub>	
	78 <i>e</i>	9/0.8	57 <i>e</i>	7/0.3
	243 <i>a</i> l	2/37	183 <i>a</i> l	0.2/40
M–N str	390 <i>a</i> l	12/4	290 <i>a</i> l	19/3
NH <sub>3</sub> roc	542 <i>e</i>	10/18	495 <i>e</i>	17/20
NH <sub>3</sub> inv	1189 <i>a</i> l	173/1	1151 <i>a</i> l	177/0.1
	1655 <i>e</i>	28/9	1659 <i>e</i>	27/10
sym N–H str	3493 <i>a</i> l	0.2/496	3512 <i>a</i> l	0.2/598
	3625 <i>e</i>	35/49	3651 <i>e</i>	31/57
	Cu <sub>3</sub> NH <sub>3</sub>		Ag <sub>3</sub> NH <sub>3</sub>	
Me tor	26 <i>a</i> ''	0/0.6	19i <i>a</i> ''	0/0.2
	40 <i>a</i> ''	2/0.2	13 <i>a</i> ''	2/0
	78 <i>d</i>	7/0.6	49 <i>d</i>	6/0.2
	152 <i>d</i>	2/4	94 <i>d</i>	1/2
	162 <i>a</i> ''	4/63	114 <i>a</i> ''	4/37
	233 <i>d</i>	2/17	168 <i>d</i>	1/18
M–N str	410 <i>d</i>	5/0.7	306 <i>d</i>	11/0.6
NH <sub>3</sub> roc'	561 <i>a</i> ''	26/36	520 <i>a</i> ''	38/9
	571 <i>d</i>	16/4	523 <i>d</i>	23/4
NH <sub>3</sub> inv	1205 <i>d</i>	180/4	1171 <i>d</i>	181/6
	1658 <i>a</i> ''	23/8	1661 <i>d</i>	22/7
	1658 <i>d</i>	30/5	1662 <i>a</i> ''	22/4
sym N–H str	3501 <i>d</i>	8/185	3517 <i>d</i>	10/234
	3627 <i>d</i>	38/46	3650 <i>d</i>	33/53
	3628 <i>a</i> ''	33/18	3651 <i>d</i> ''	30/48

<sup>2</sup> See Table 29.1 from *Physical Chemistry*, 4th edn., by P.W. Atkins: the largest enthalpy of physisorption listed for  $\text{NH}_3$  is  $-38$  kJ/mol =  $9.1$  kcal/mol.

Table 5

Harmonic frequencies ( $\text{cm}^{-1}$ ), IR intensities (IR, in  $\text{km/mol}$ ) and Raman intensities (Ram, in  $\text{\AA}^4/\text{a.m.u.}$ ) of  $\text{Cu}_n(\text{NH}_3)_m$  and  $\text{Ag}_n(\text{NH}_3)_m$  ( $n = 4, m = 1, 2$ )

	$\omega$	IR/Ram	$\omega$	IR/Ram
	$\text{Cu}_4\text{NH}_3$		$\text{Ag}_4\text{NH}_3$	
NH <sub>3</sub> tor	43 $d'$	0.7/1	27 $d'$	0.4/0.5
	55 $d'$	1/0.2	36 $d'$	1/0.1
	69 $d''$	3/1	40 $d''$	3/1
	82 $d'$	7/0.1	51 $d'$	5/0
	116 $d'$	4/1	80	3/0.7
	144 $d''$	0.4/10	99 $d''$	0.3/8
	154 $d'$	0.7/23	108 $d'$	0.3/30
	235 $d''$	9/0.8	164 $d''$	7/0.4
	245 $d'$	0.2/36	179 $d'$	0.1/30
M–N str	408 $d'$	4/2	311 $d'$	8/3
NH <sub>3</sub> roo $\nu'$	566 $d''$	10/12	525 $d'$	19/2
	567 $d'$	14/2	526 $d''$	14/8
NH <sub>3</sub> inv	1194 $d'$	185/3	1162 $d'$	184/7
	1657 $d''$	20/7	1660 $d''$	19/7
	1658 $d'$	31/4	1661 $d'$	29/4
sym N–H str	3507 $d'$	8/156	3521 $d'$	11/178
	3633 $d'$	35/39	3654 $d'$	31/45
	3638 $d''$	30/20	3657 $d''$	24/30
	$\text{Cu}_4\text{NH}_3$ (L)		$\text{Ag}_4\text{NH}_3$ (L)	
NH <sub>3</sub> tor	9 $d'$	0.1/0.6	23 $d''$	0.3/0
	33 $d'$	4/4	32 $d''$	4/3
	33i $d''$	7/2	33 $d'$	2/2
	88 $d'$	4/0.1	64 $d'$	5/1
	103 $d''$	0.1/2	71 $d''$	0.9/0.1
	110 $d''$	6/0.1	76 $d''$	4/0
	149 $d'$	0.3/31	107 $d'$	0.3/45
	213 $d'$	12/0.5	155 $d'$	10/0.7
	284 $d'$	0.7/24	197 $d'$	0.2/26
M–N str	313 $d'$	18/0.5	244 $d'$	32/4
NH <sub>3</sub> roo $\nu'$	471 $d''$	2/13	431 $d''$	7/15
	488 $d'$	8/11	436 $d'$	14/22
NH <sub>3</sub> inv	1172 $d'$	197/204	1128 $d'$	204/0.5
	1656 $d'$	27/3	1658 $d''$	26/9
	1656 $d''$	28/3	1659 $d'$	26/10
sym N–H str	3481 $d'$	23/1100	3500 $d'$	11/1829
	3620 $d''$	26/43	3644 $d''$	22/84
	3621 $d'$	28/50	3646 $d'$	23/94
	$\text{Cu}_4(\text{NH}_3)_2$		$\text{Ag}_4(\text{NH}_3)_2$	
M–N str $\nu'$	366 $\nu_{28}$ ( $b_2$ )	10/0	290 $\nu_{28}$ ( $b_2$ )	17/0.01
	390 $\nu_6$ ( $a_1$ )	0/5	306 $\nu_6$ ( $a_1$ )	0/5
NH <sub>3</sub> roo $\nu''''$	525 $\nu_{13}$ ( $a_2$ )	0/32	495 $\nu_{13}$ ( $a_2$ )	0/20
	529 $\nu_5$ ( $a_1$ )	20/2	496 $\nu_5$ ( $a_1$ )	33/0.4
	537 $\nu_{27}$ ( $b_2$ )	0.2/7	501 $\nu_{27}$ ( $b_2$ )	0/6
	548 $\nu_{19}$ ( $b_1$ )	24/0	513 $\nu_{19}$ ( $b_1$ )	33/0
NH <sub>3</sub> inv $\nu'$	1166 $\nu_{26}$ ( $b_2$ )	416/0.1	1140 $\nu_{26}$ ( $b_2$ )	405/0.1
	1168 $\nu_4$ ( $a_1$ )	0/14	1142 $\nu_4$ ( $a_1$ )	0.04/19
sym N–H str $\nu'$	3506 $\nu_{24}$ ( $b_2$ )	6/0.1	3521 $\nu_{24}$ ( $b_2$ )	11/06
	3506 $\nu_2$ ( $a_1$ )	0/399	3521 $\nu_2$ ( $a_1$ )	0/416

‘umbrella’) frequency upon complexation (in  $\text{cm}^{-1}$ ): 119 (theory) versus 115 (experiment, Ref. [1]) for  $\text{Ag}_2\text{NH}_3$ ; 130 versus a lower bound of 140 for  $\text{Ag}_4\text{NH}_3$ ; and 109 versus 115 for  $\text{Ag}_4(\text{NH}_3)_2$ . Our calculations show a correlation between the blue shift in inversion mode frequency and binding enthalpy, but no such correlation is apparent among the experimental data [1]. The theoretical values for  $\Delta S_{\text{ad}}$  for structures S and L are similar. The experimental value of  $\Delta S_{\text{ad}}$  is  $-24 \text{ cal mol}^{-1} \text{ K}^{-1}$  which agrees well with both computed values. Thus, although the calculated enthalpies indicate that  $\text{Ag}_4\text{NH}_3$  (S) and  $\text{Ag}_4(\text{NH}_3)_2$  (SS) are the thermodynamically favoured isomers, we cannot make a definitive assignment of the observed species.

#### 4. Vibrational modes and spectroscopic properties

The computed harmonic frequencies and IR and Raman intensities for the vibrational modes of the cluster complexes are given in Tables 4 and 5. For  $\text{M}_n(\text{NH}_3)_2$  we show only selected vibrations and label them by the Herzberg order [24]. Vibrations of the  $\text{NH}_3$  ligand fall in the  $1000\text{--}3600 \text{ cm}^{-1}$  range and are well separated from the low frequency vibrations in the  $20\text{--}300 \text{ cm}^{-1}$  range characteristic of the metal clusters. Additional vibrational modes in the  $0\text{--}600 \text{ cm}^{-1}$  range arise from binding between  $\text{M}_n$  and  $\text{NH}_3$ . In the spectrum of  $\text{MNH}_3$  a doubly degenerate rocking mode of  $\text{NH}_3$  and a metal–ligand (M–N) stretching mode are observed. In  $\text{M}_2\text{NH}_3$ , degenerate metal–ligand bending modes show up. In addition, binding of  $\text{NH}_3$  to a non-linear  $\text{M}_n$  cluster gives rise to a torsional mode of  $\text{NH}_3$  which is found to be the lowest frequency mode. Three of these low frequency vibrational modes are assigned as M–N

stretch,  $\text{NH}_3$  rocking and  $\text{NH}_3$  torsion. Of the modes associated with the  $\text{NH}_3$  ligand, we assign only the inversion mode and the totally symmetric N–H stretch. The calculated normal modes of  $\text{Cu}_n\text{NH}_3$  and  $\text{Ag}_n\text{NH}_3$  are similar and the energy ordering is the same in the two series. Therefore, we list them together. We get small imaginary frequencies for the  $\text{NH}_3$  torsional motion of  $\text{Ag}_3\text{NH}_3$  and a bending mode of  $\text{Cu}_4\text{NH}_3$  (L). However, these imaginary frequencies are clearly an artificial result. They are due to small numerical errors which are common in DFT because of the need for numerical integration in calculating some terms of the energy.

Spectroscopic measurement of  $\text{M}_n$  has focused on the peak corresponding to the  $\text{NH}_3$  inversion [1]. Computed *harmonic* frequencies for this mode for  $\text{Ag}_2\text{NH}_3$ ,  $\text{Ag}_4\text{NH}_3$  and  $\text{Ag}_4(\text{NH}_3)_2$  are larger than the observed *fundamentals* (Table 2 of Ref. [1]) by about 5–10% which is reasonable. As we mentioned, there is good agreement between the calculated and observed shift in that mode’s frequency relative to free ammonia. We predict a blue shift for the inversion vibration as the size of  $\text{M}_n$  increases from 1 to 3, and then a red shift by about  $10 \text{ cm}^{-1}$  for  $\text{M}_4\text{NH}_3$  (S). The  $\text{NH}_3$  rocking mode also shifts to higher frequency as  $n$  increases from 1 to 3, and then shifts to lower values for  $\text{M}_4\text{NH}_3$  (L), but increases for  $\text{M}_4\text{NH}_3$  (S). Binding of a second  $\text{NH}_3$  to  $\text{M}_4\text{NH}_3$  (S) makes the inversion vibration nearly doubly degenerate, the ‘in-phase’ ( $a_1$ ) and ‘out-of-phase’ ( $b_2$ ) modes being only  $2 \text{ cm}^{-1}$  apart. The  $b_2$  peak has a predicted IR intensity twice as large as the single inversion vibration in  $\text{M}_4\text{NH}_3$ .

Raman scattering intensities offer a possible means of structural assignment of  $\text{M}_4\text{NH}_3$  and  $\text{M}_4(\text{NH}_3)_2$ . The most noticeable feature in the computed Raman spectra of  $\text{M}_n(\text{NH}_3)_m$  is a strong Raman signal for

Table 6  
Natural population atomic charges for  $\text{M}_4$  and  $\text{M}_4\text{NH}_3$

	$\text{Cu}_4$	$\text{Cu}_4\text{NH}_3$ (S)	$\text{Cu}_4\text{NH}_3$ (L)	$\text{Ag}_4$	$\text{Ag}_4\text{NH}_3$ (S)	$\text{Ag}_4\text{NH}_3$ (L)
Q(M1)	+0.279	+ .365	+0.248	+0.297	+0.369	+0.270
Q(M2)	+0.279	+ .171	+0.248	+0.297	+0.203	+0.270
Q(M3)	-0.279	-0.301	-0.095	-0.297	-0.316	-0.154
Q(M4)	-0.279	-0.301	-0.436	-0.297	-0.316	-0.424
Q(N)		-1.177	-1.196		-1.175	-1.179
Q( $\text{NH}_3$ )		+0.065	+0.034		+0.061	+0.036

the totally symmetric N–H stretching mode. The Raman intensity of this mode shows a high sensitivity to the metal cluster size and binding site. It is  $109 \text{ \AA}^4/\text{a.m.u.}$  in free  $\text{NH}_3$  and it increases by factors of: 11 on binding to Cu; 7 on binding to Ag; about 5 on binding to either  $\text{Cu}_2$  or  $\text{Ag}_2$ ; 10 in  $\text{Cu}_4\text{NH}_3$  (L) and 17 in  $\text{Ag}_4\text{NH}_3$  (L), but only about 2 in  $\text{Cu}_4\text{NH}_3$  (S) and  $\text{Ag}_4\text{NH}_3$  (S); and 1.5–2 (per  $\text{NH}_3$  ligand) in  $\text{M}_3\text{NH}_3$  and  $\text{M}_4(\text{NH}_3)_2$  complexes. Thus, it may be possible to assign the adsorption site of  $\text{NH}_3$  on clusters by looking at ratios of peak intensities. Generally, Raman intensities depend on molecular polarizabilities. For metal clusters, a large intensity enhancement of the symmetric N–H stretch would normally indicate that the metal–N bond is aligned with the longer (more polarizable) axis of the cluster.

## 5. Further analysis

We now characterize the electron density distribution by examining partial atomic charges obtained from a natural population analysis (NPA) [25] (see Table 6). The NPA has the advantage of having only a small basis set dependence [26]. For  $\text{Cu}_4$  and  $\text{Ag}_4$ , the two atoms at the end of the short diagonal carry positive charges of about +0.3 while corresponding negative charges reside on the two atoms of the long diagonal. The N atom carries a negative charge of  $-1.123$  in free  $\text{NH}_3$ . Binding of  $\text{NH}_3$  to  $\text{Cu}_4$  or  $\text{Ag}_4$  results in a very small transfer of electron ( $\approx 0.03$ – $0.06$ ) from the ligand to the cluster, but a significant charge redistribution within the cluster. The greater stability of the S isomer of  $\text{M}_4(\text{NH}_3)$  over the L isomer can be understood as due to binding of the *negatively* charged N atom of  $\text{NH}_3$  to one of the *positively* charged metal atoms. The NPA charges on atoms M1 and M2 for the S isomer, and atoms M3 and M4 for the L isomer, show that polarization of the metal cluster electron density away from the  $\text{NH}_3$  ligand is also an important aspect of the interaction. Because NPA charges can be obtained at a low cost, it may be possible to predict the binding site of  $\text{NH}_3$  or similar ligands on large metal cluster without doing many costly cluster–ligand complex calculations. We are currently investigating this possible use of the NPA.

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